

3- fazni sistem

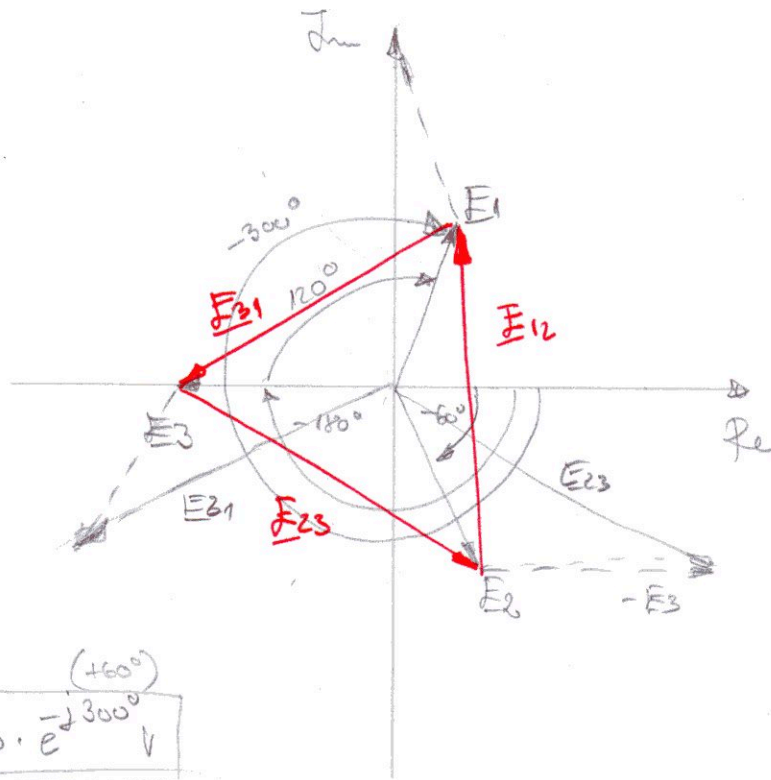
$$m=3$$

$$\underline{E}_2 = 200 \cdot e^{-j60^\circ} \text{ V}$$

$$\alpha = \frac{2\pi}{m} = \frac{2\pi}{3} = 120^\circ$$

$$\begin{aligned} \underline{E}_3 &= \underline{E}_2 \cdot e^{j120^\circ} \\ &= 200 \cdot e^{-j180^\circ} \text{ V} \end{aligned}$$

$$\underline{E}_1 = \underline{E}_3 \cdot e^{j120^\circ} = 200 \cdot e^{-j300^\circ} \text{ V}$$



$$\underline{E}_{12} = \underline{E}_1 - \underline{E}_2 = 200 \cdot e^{j60^\circ} - 200 \cdot e^{-j60^\circ}$$

$$= 200 \cdot \frac{1}{2} + j200 \cdot \frac{\sqrt{3}}{2} - \left(200 \cdot \frac{1}{2} - j200 \cdot \frac{\sqrt{3}}{2} \right)$$

$$= j100\sqrt{3} + j100\sqrt{3} = 200\sqrt{3} \cdot e^{j90^\circ} \text{ V}$$

$$\underline{E}_{23} = \underline{E}_2 - \underline{E}_3 = \underline{E}_2 \cdot \sqrt{3} \cdot e^{j30^\circ} = 200 \cdot \sqrt{3} \cdot e^{-j60^\circ} \cdot e^{j30^\circ} = 200\sqrt{3} \cdot e^{j30^\circ} \text{ V}$$

$$\underline{E}_{31} = \underline{E}_3 - \underline{E}_1 = \underline{E}_3 \cdot \sqrt{3} \cdot e^{j30^\circ} = 200 \cdot \sqrt{3} \cdot e^{-j180^\circ} \cdot e^{j30^\circ} = 200 \cdot e^{-j150^\circ} \text{ V}$$

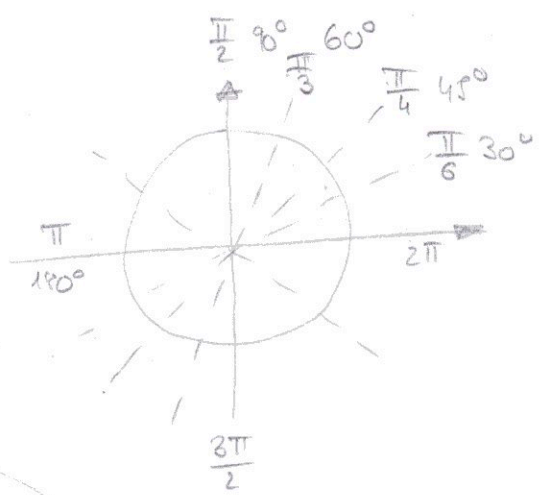
$$m=6$$

$$\alpha = \pm k \frac{2\pi}{m}$$

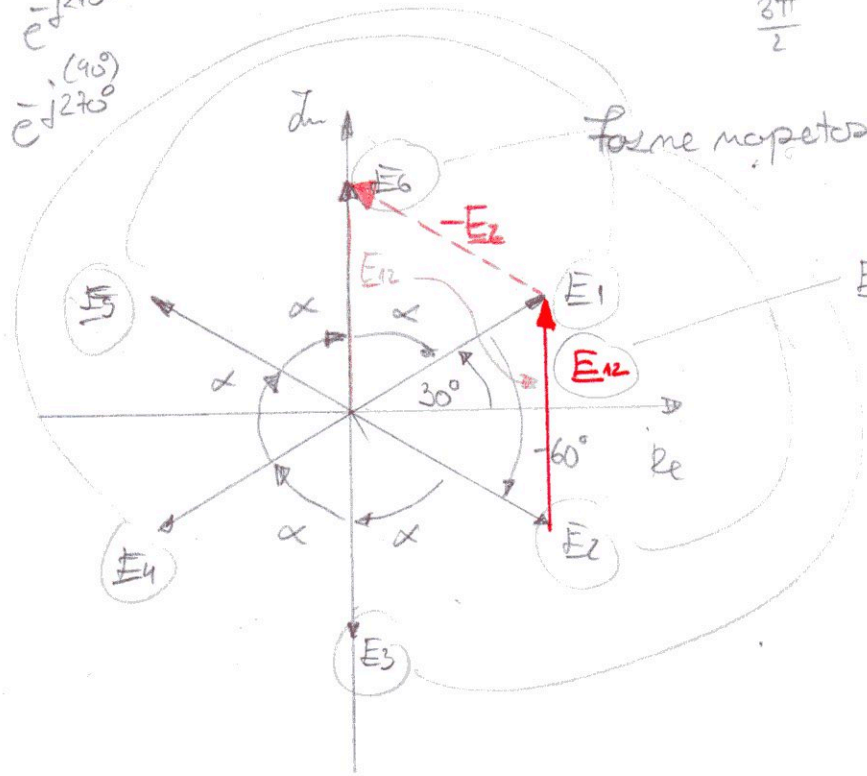
$\alpha = \pm k \frac{2\pi}{6} = \pm k \frac{\pi}{3} = \pm k 60^\circ$ za tu lot zaostaja, vsaka naslednja napetost za E_1 , (matematično negativna smer, je smer uinrega lokalca)

$$E_1 = 100 \cdot e^{j30^\circ} V$$

$$E_2 = E_1 \cdot e^{j60^\circ} = 100 \cdot e^{j90^\circ} V$$



- $E_3 = 100 \cdot e^{j120^\circ}$
- $E_4 = 100 \cdot e^{j150^\circ}$
- $E_5 = 100 \cdot e^{j210^\circ}$
- $E_6 = 100 \cdot e^{j270^\circ}$



$$E_{12} = E_1 - E_2$$

$$(E_1 + (-E_2))$$



$$m=3$$

$$\alpha = \pm k \frac{2\pi}{m} \Rightarrow \alpha = \frac{2\pi}{3} = \boxed{120^\circ}$$

$$\underline{E_{12}} = 400 \cdot e^{-j150^\circ} \text{ V}$$

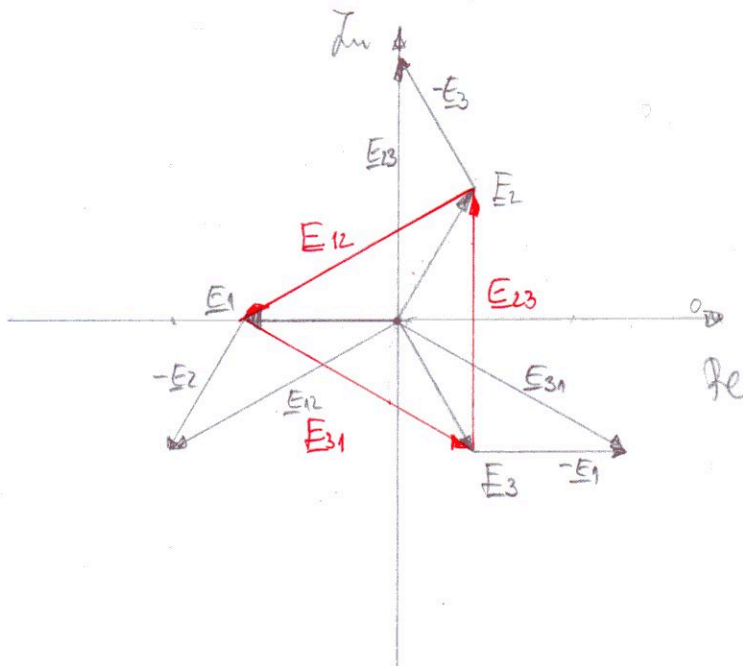
$$E_{12} = E_1 \cdot \sqrt{3} \cdot e^{j30^\circ} \rightarrow E_1 = \frac{E_{12}}{\sqrt{3} \cdot e^{j30^\circ}} = \boxed{\frac{400}{\sqrt{3}} \cdot e^{-j180^\circ} \text{ V}}$$

$$E_{23} = E_2 \cdot \sqrt{3} \cdot e^{j30^\circ} = E_1 \cdot \sqrt{3} \cdot e^{j90^\circ} = \boxed{400 \cdot e^{j270^\circ} \text{ V}}$$

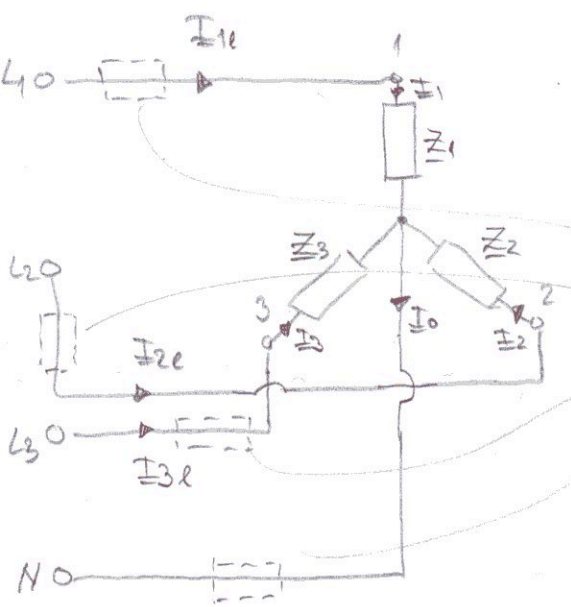
$$E_2 = E_1 \cdot e^{j120^\circ} = \boxed{\frac{400}{\sqrt{3}} \cdot e^{j300^\circ} \text{ V}}$$

$$E_3 = E_2 \cdot e^{j120^\circ} = \boxed{\frac{400}{\sqrt{3}} \cdot e^{j60^\circ} \text{ V}}$$

$$E_1 = E_3 \cdot \sqrt{3} \cdot e^{j30^\circ} = \boxed{400 \cdot e^{j30^\circ} \text{ V}}$$



• URAVNOLIŽEN SISTEM (Breme to eula)



$$Z_1 = Z_2 = Z_3$$

$$I_0 = I_1 + I_2 + I_3 = 0 \text{ ce je breme simetrično}$$

Možne so impedanca linij

$$E_1 = 100 \text{ V}$$

$$Z_1 = Z_2 = Z_3 = 10 + j10 \Omega$$

$$I_1, I_2, I_3 = ?$$

$$I_1 = \frac{E_1}{Z_1} = \frac{100}{10 + j10} = \frac{100}{10\sqrt{2} \cdot e^{j45^\circ}} = \underline{5\sqrt{2} \cdot e^{j45^\circ} \text{ A}}$$

$$\sqrt{10^2 + 10^2} = \sqrt{200} = 10\sqrt{2}$$

$$\tan \varphi = \frac{10}{10} = 1 \quad \varphi = 45^\circ$$

$$I_2 = \frac{E_2}{Z_2} = \frac{E_1 \cdot e^{j120^\circ}}{10\sqrt{2} \cdot e^{j45^\circ}} = \underline{5\sqrt{2} \cdot e^{j165^\circ} \text{ A}}$$

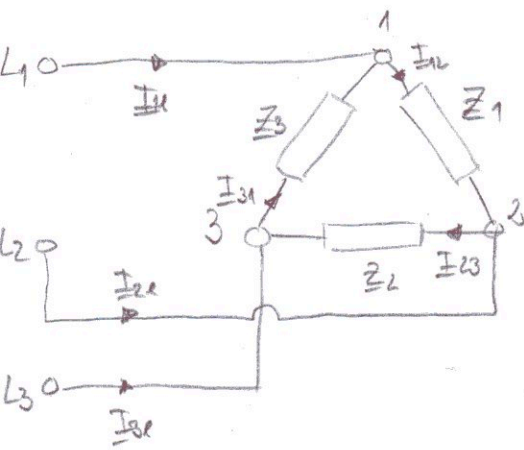
$$I_3 = \frac{E_3}{Z_3} = \frac{100 \cdot e^{j240^\circ}}{10\sqrt{2} \cdot e^{j45^\circ}} = 5\sqrt{2} \cdot e^{j285^\circ} = \underline{5\sqrt{2} \cdot e^{j75^\circ} \text{ A}}$$



NEŠIMETRIČNA OBREMENITRA

$$I_1 = \frac{E_1}{Z_1} = \frac{E_2}{Z_2} = \dots$$

U_0 - prazna nestručna
baza



Buena N nodita,
reputat na buena

$$U_1 = E_1 - U_0,$$

$$U_2 = E_2 - U_0, \dots$$

RACUNAMO LAHKO LEI $\Delta - \Delta$!
 $\lambda - \lambda$!

$$Z_{12} = 10 \Omega$$

$$Z_{23} = j 10 \Omega$$

$$Z_{31} = -j 10 \Omega$$

medfaze

$$E_1 = 100 \cdot e^{j60^\circ} \text{ V}$$

fazant matruko v medfaze!

$$m=3$$

$$\alpha = \frac{2\pi}{m} = 120^\circ$$

$$I_1, I_2, I_3 = ?$$

$$E_{12} = E_1 \cdot \sqrt{3} \cdot e^{j30^\circ} = 100\sqrt{3} \cdot e^{j90^\circ} \text{ V}$$

$$E_{23} = E_{12} \cdot e^{j120^\circ} = 100\sqrt{3} \cdot e^{j30^\circ} \text{ V}$$

$$E_{31} = E_{23} \cdot e^{j120^\circ} = 100\sqrt{3} \cdot e^{j150^\circ} \text{ V}$$

$$I_{12} = \frac{E_{12}}{Z_{12}} = \frac{100\sqrt{3} \cdot e^{j90^\circ}}{10 \Omega} = 10\sqrt{3} \cdot e^{j90^\circ} \text{ A}$$

$$I_{23} = \frac{E_{23}}{Z_{23}} = \frac{100\sqrt{3} \cdot e^{j30^\circ}}{j10} = \frac{100\sqrt{3} \cdot e^{j30^\circ}}{10 \cdot e^{j90^\circ}} = 10\sqrt{3} \cdot e^{j120^\circ} \text{ A}$$

$$I_{31} = \frac{E_{31}}{Z_{31}} = \frac{100\sqrt{3} \cdot e^{j150^\circ}}{10 \cdot e^{j90^\circ}} = 10\sqrt{3} \cdot e^{j60^\circ} \text{ A}$$

$I_1, I_2, I_3 \rightarrow$ Kirchhoff

$$I_1 = I_{12} - I_{31} = -8,66 + j 32,32 \text{ A}$$

$$I_2 = I_{23} - I_{12} = -8,66 - j 32,32 \text{ A}$$

$$I_3 = I_{31} - I_{23} = 17,32 \text{ A}$$

$\Sigma = \emptyset$ Buena N.



• MNODIŠKOVNA VEZAVA (Δ)

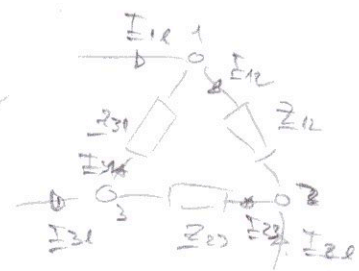
$E_{12} = 300 \cdot e^{j90^\circ} V$
 $Z_{12} = j20 \Omega$
 $Z_{23} = 20 \Omega$
 $Z_{31} = -j20 \Omega$

$I_{12} = \frac{E_{12}}{Z_{12}} = \frac{300 \cdot e^{j90^\circ}}{j20 \cdot e^{j90^\circ}} = 15 A$
 $I_{23} = \frac{E_{23}}{Z_{23}} = \frac{15 \cdot 300 \cdot e^{j30^\circ}}{20} = 15 \cdot e^{-j30^\circ} A$
 $I_{31} = \frac{E_{31}}{Z_{31}} = \frac{15 \cdot 300 \cdot e^{j150^\circ}}{20 \cdot e^{j90^\circ}} = 15 \cdot e^{j60^\circ} A$

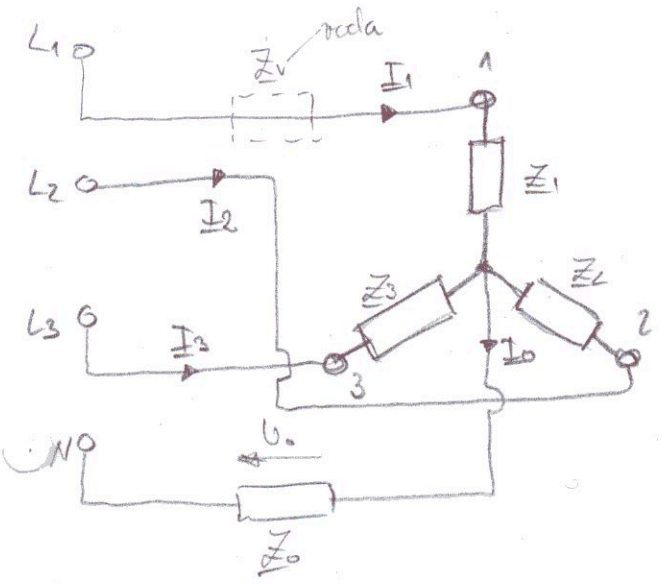
$I_1, I_2, I_3 = ?$

$I_1 = I_{12} - I_{31} = 7,5 + j12,99 A$
 $I_2 = I_{23} - I_{12} = -2,01 - j7,5 A$
 $I_3 = I_{31} - I_{23} = -5,49 - j5,49 A$

$\Sigma = \phi \checkmark$



• VEŠKRAKA VEZAVA (Y)



$I_{linijskega} = I_{bremenocene}$

- Če je breme unarmotorno U_0 zaneseno
 Sg je $I_0 = \phi$.

$Z_1 = Z_2 = Z_3$
 $I_0 = I_1 + I_2 + I_3 = \phi$
 U_0 - zaneseno
 $U_1 = E_1$

memorandžen sistem

- brez N_j

$E_1 = U_1 + U_0$
 $\Rightarrow U_1 = E_1 - U_0$

$$U_0 Y_0 = \underbrace{(E_1 - U_0) Y_1}_{I_1} + \underbrace{(E_2 - U_0) Y_2}_{I_2} + \dots + \underbrace{(E_n - U_0) Y_n}_{I_n}$$

$I_0 = I_1 + I_2 + I_3 + \dots + I_n$
 $U_0 = I_0 \cdot Z_0$
 $I_1 = U_1 \cdot Y_1$
 $I_n = U_n \cdot Y_n$

$$\Rightarrow U_0 = \frac{E_1 Y_1 + E_2 Y_2 + \dots + E_n Y_n}{(Y_0) + Y_1 + Y_2 + \dots + Y_n}$$



• NEUDAVNOTELEN SISTEMI ZN.

1

$$\underline{E}_1 = 200 \cdot e^{j300} \text{ V}$$

$$\underline{Z}_1 = j20 \Omega$$

$$\underline{Z}_2 = 20 \Omega$$

$$\underline{Z}_3 = -j20 \Omega$$

linijski tok?

$$\underline{E}_1 = \underline{U}_1$$

$$\underline{E}_2 = \underline{U}_2$$

$$\underline{E}_3 = \underline{U}_3$$

$$\underline{I}_1 = \frac{\underline{U}_1}{\underline{Z}_1} = \frac{200 \cdot e^{j30^\circ}}{20 \cdot e^{j90^\circ}} = \boxed{10 \cdot e^{j60^\circ} \text{ A}}$$

$$\underline{I}_2 = \frac{\underline{U}_2}{\underline{Z}_2} = \frac{200 \cdot e^{j90^\circ}}{20} = \boxed{10 \cdot e^{j90^\circ} \text{ A}}$$

$$\underline{I}_3 = \frac{\underline{U}_3}{\underline{Z}_3} = \frac{200 \cdot e^{j210^\circ}}{20 \cdot e^{j90^\circ}} = \boxed{10 \cdot e^{j120^\circ} \text{ A}}$$

$$\underline{I}_0 = \underline{I}_1 + \underline{I}_2 + \underline{I}_3 = \boxed{-j27,32 \text{ A}}$$

• BLEZ N

- presnehitelj \underline{U}_0

$$\underline{U}_0 = \frac{\underline{E}_1 \underline{Y}_1 + \underline{E}_2 \underline{Y}_2 + \underline{E}_3 \underline{Y}_3}{\underline{Y}_1 + \underline{Y}_2 + \underline{Y}_3} = \frac{\underline{I}_0}{\underline{Y}_1 + \underline{Y}_2 + \underline{Y}_3} = \frac{-j27,32}{0,05} = \boxed{-546,41 \text{ V}}$$

$$\underline{U}_1 = \underline{E}_1 - \underline{U}_0$$

$$\underline{U}_2 = \underline{E}_2 - \underline{U}_0$$

$$\underline{U}_3 = \underline{E}_3 - \underline{U}_0$$

$$\underline{I}_1 = \frac{\underline{U}_1}{\underline{Z}_1} = \frac{669,213 \cdot e^{j75^\circ}}{20 \cdot e^{j90^\circ}} = \boxed{32,32 - j8,66 \text{ A}}$$

$$\underline{U}_1 = 200 \cdot e^{j30^\circ} + 546,41 \text{ V} = 173,21 + j646,4 \text{ V} = 669,213 \cdot e^{j75^\circ}$$

$$\underline{I}_2 = \frac{346,41 \cdot e^{j90^\circ}}{20} = \boxed{j17,32 \text{ A}}$$

$$\underline{I}_3 = \frac{669,213 \cdot e^{j105^\circ}}{20 \cdot e^{j90^\circ}} = \boxed{-32,32 - j8,66 \text{ A}}$$

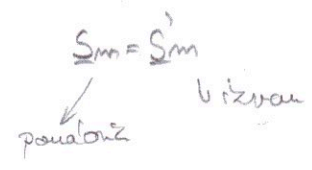


• MOĆI V 3-Ź DISTANCIH

S - moćta kompleksna!

rešenje 1:

$S_{m} = \underline{U}_m \cdot \underline{I}_m^*$ IZUOR; $S_m' = \underline{E}_m \cdot \underline{I}_m^*$



- Skupna delovna moć P

$P = P_1 + P_2 + P_3 \dots$
 $= U_1 \cdot I_1 \cdot \cos \varphi_1 + U_2 \cdot I_2 \cdot \cos \varphi_2 + U_3 \cdot I_3 \cdot \cos \varphi_3 + \dots$
 $= I_1^2 R_1 \cdot \cos \varphi_1 + I_2^2 R_2 \cdot \cos \varphi_2 + \dots$

$Q = Q_1 + Q_2 + Q_3 \dots$
 $= U_1 \cdot I_1 \cdot \sin \varphi_1 + U_2 \cdot I_2 \cdot \sin \varphi_2 + \dots$

Unermotazan sistem

$E = \sqrt{3} \cdot E_f$ $I = I_f = I_e$ $\varphi_1 = \varphi_2 = \varphi_3$
 ↓
 medifazna napetost
 $S = 3S_1 = 3E_1 I_1 = \sqrt{3} EI$ ← linijalni dol

rešenje 2

$S = S_{12} + S_{23} + S_{31} = \underline{E}_{12} \cdot \underline{I}_{12}^* + \underline{E}_{23} \cdot \underline{I}_{23}^* + \underline{E}_{31} \cdot \underline{I}_{31}^* + \dots = P + jQ$

$P = E_{12} \cdot I_{12} \cdot \cos \varphi_{12} + E_{23} \cdot I_{23} \cdot \cos \varphi_{23} + \dots$

$Q = E_{12} \cdot I_{12} \cdot \sin \varphi_{12} + \dots$

Unermotazan sistem

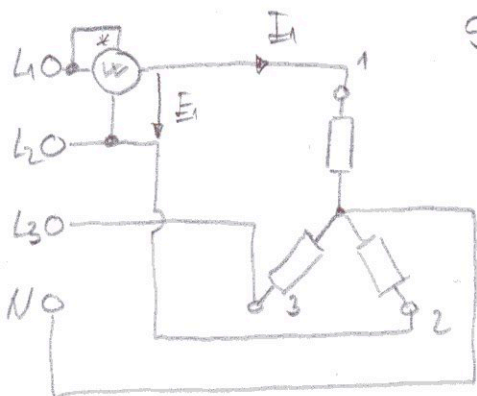
$E_{br} = E$ $I = \sqrt{3} I_f$ $\varphi_1 = \varphi_2 = \varphi_3$

$S = 3 E_{br} I_{12} = \sqrt{3} EI$



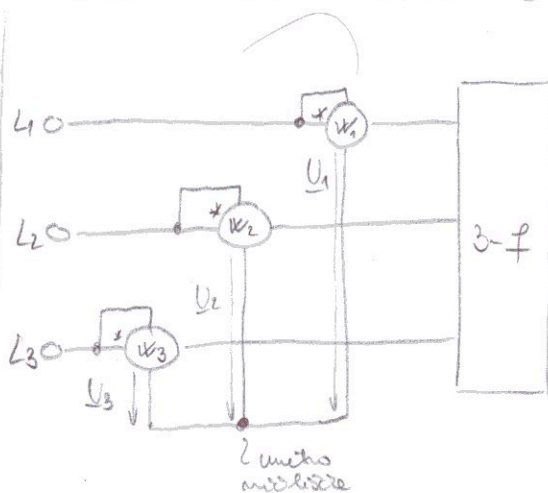
• MERITEV W IZRAČUN MOČI U 3-f

- Unanofazni sistem



$$S = 3S_1 = 3 \cdot E_1 \cdot I_1^*$$

- Nemanofazni sistem (baza N)



$$U_1 = E_1 - U_0, \quad U_2 = E_2 - U_0, \quad U_3 = E_3 - U_0$$

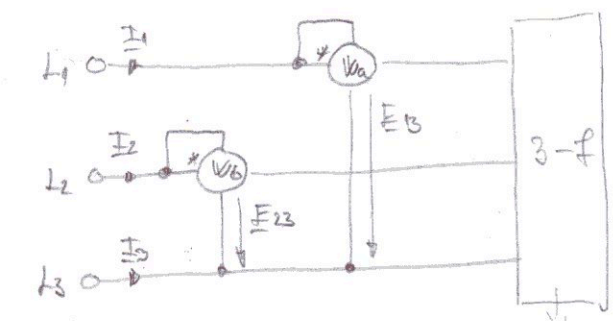
$$S = U_1 I_1^* + U_2 I_2^* + U_3 I_3^*$$

$$= (E_1 - U_0) \cdot I_1^* + (E_2 - U_0) I_2^* + (E_3 - U_0) I_3^*$$

$$= E_1 I_1^* + E_2 I_2^* + E_3 I_3^*$$

$\leftarrow U_0 = \phi$

- Meritev moči s 2 wattmetromi



$$S_a = E_{13} \cdot I_1^* = (E_1 - E_3) I_1^* = E_1 I_1^* - E_3 I_1^*$$

$$S_b = E_{23} I_2^* = (E_2 - E_3) I_2^* = E_2 I_2^* - E_3 I_2^*$$

$$S_a + S_b = E_1 I_1^* + E_2 I_2^* - E_3 (I_1^* + I_2^*)$$

$$= E_1 I_1^* + E_2 I_2^* + E_3 I_3^*$$

$$I_1 + I_2 + I_3 = 0$$

$$-I_3 = I_1 + I_2$$

W-metromi \rightarrow rezultati del moči!

$3-f \Rightarrow \underline{\underline{\alpha = 120^\circ}}$

$E_{L3} = 100\sqrt{3} V$

$Z_1 = 10 \Omega$

$Z_2 = j5 \Omega$

$Z_3 = -j25 \Omega$

$I_1, I_2, I_3 = ?$

$E_{31} = E_{23} \cdot e^{j120^\circ} = 100\sqrt{3} \cdot e^{j120^\circ} V$

$E_{12} = E_{31} \cdot e^{j120^\circ} = 100\sqrt{3} \cdot e^{j120^\circ} V$

transformirano u Δ

$\lambda \rightarrow \Delta$

$\underline{Z} = Z_1 + Z_2 + \frac{Z_1 Z_2}{Z_3}$

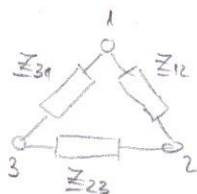
Enačbe transformacij

$\lambda \rightarrow \Delta$

$\underline{Z} = Z_1 + Z_2 + \frac{Z_1 Z_2}{Z_3}$

$\Delta \rightarrow \lambda$

$\underline{Z} = \frac{Z_1 + Z_2}{Z_1 + Z_2 + Z_3}$



$Z_{12} = Z_1 + Z_2 + \frac{Z_1 Z_2}{Z_3} = 10 + j5 - \frac{j50}{j25} = 8 + j5 \Omega$

$Z_{23} = Z_2 + Z_3 + \frac{Z_2 Z_3}{Z_1} = -j20 + \frac{125}{10} = 12,5 - j20 \Omega$

$Z_{31} = Z_3 + Z_1 + \frac{Z_3 Z_1}{Z_2} = 10 - j25 + \frac{-j250}{j5} = 40 - j25 \Omega$

$I_{12} = \frac{E_{12}}{Z_{12}} = \frac{100\sqrt{3} \cdot e^{j120^\circ}}{8 + j5} = 0,64 + j18,35 A$

$I_{23} = \frac{E_{23}}{Z_{23}} = \frac{100\sqrt{3}}{12,5 - j20} = 3,89 + j6,23 A$

$I_{31} = \frac{E_{31}}{Z_{31}} = \frac{100\sqrt{3} \cdot e^{j120^\circ}}{40 - j25} = 3,24 - j1,72 A$

$I_1, I_2, I_3 \Rightarrow$ Kirchhoff

$I_1 = I_{12} - I_{31} = -2,5998 + j16,6249 A$

$I_3 = I_{31} - I_{23} = -0,65 - j4,5041 A$

$I_2 = I_{23} - I_{12} = 3,2499 - j12,1209 A$

$\Sigma = 0 \checkmark$



- pitanje 2.

$$\underline{E}_1 = 100 \cdot e^{j60^\circ} \text{ V}$$

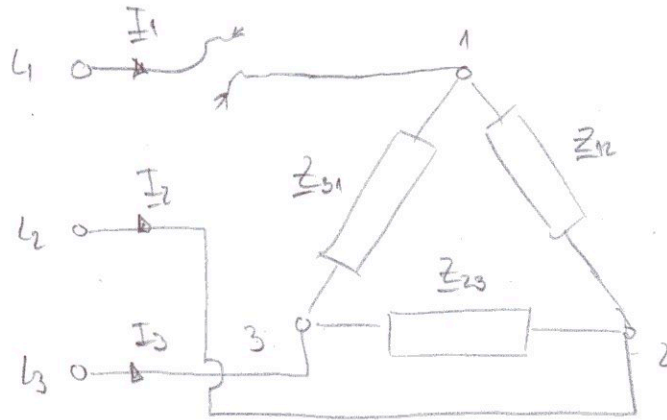
$$\underline{Z}_{12} = -j5 \Omega$$

$$\underline{Z}_{23} = 4 - j2 \Omega$$

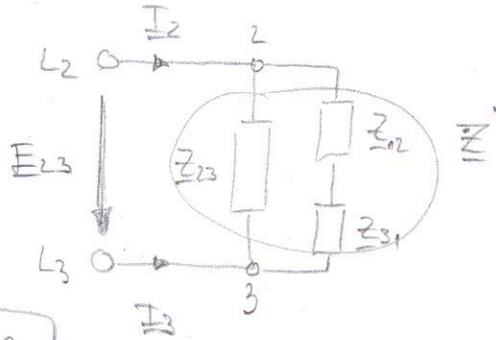
$$\underline{Z}_{31} = 2 - j4 \Omega$$

prilici det devoda 1.

I_3 po obrascu?



Po obrascu!



$$\underline{Z}' = \frac{(\underline{Z}_{12} + \underline{Z}_{31}) \cdot \underline{Z}_{23}}{\underline{Z}_{12} + \underline{Z}_{31} + \underline{Z}_{23}}$$

$$\underline{Z}' = \frac{(2 - j4) \cdot (4 - j2)}{6 - j11} = \underline{2,42 - j2,23 \Omega}$$

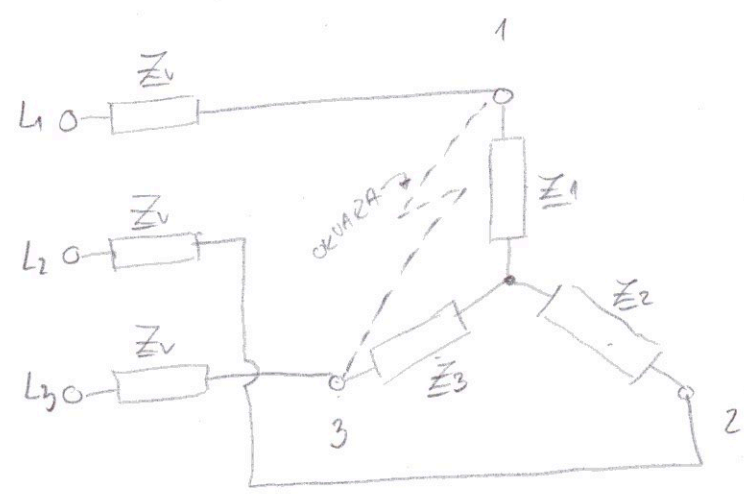
$$\underline{E}_{23} = \underline{E}_1 \cdot \frac{e^{j120^\circ}}{e^{j30^\circ}} = \underline{100\sqrt{3} \cdot e^{j150^\circ} \text{ V}}$$

$$\underline{I}_3 = -\underline{I}_2 = \frac{\underline{E}_{23}}{\underline{Z}'} = \underline{-15,7 - j50,2 \text{ A}}$$

- OZVARA

$E_{R1} = 100\sqrt{3} \cdot e^{j60^\circ} \text{ V}$
 $Z_1 = Z_2 = Z_3 = 8 + j8 \Omega (\lambda)$
 $Z_V = 2 + j2 \Omega$

I_1 , pred im po obrani!

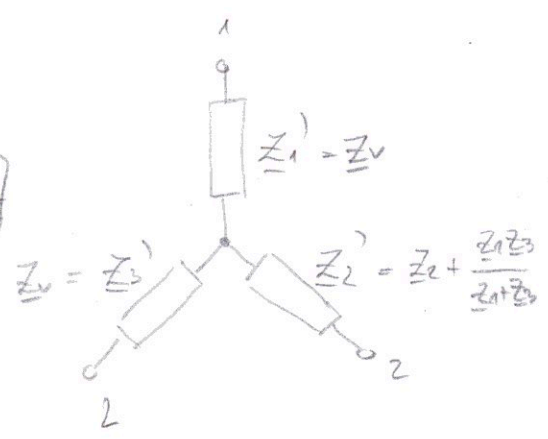


Pred: 1

$E_1 = \frac{E_{R1}}{\sqrt{3}} = \frac{100 \cdot e^{j30^\circ}}{\sqrt{3}} = 100 \cdot e^{j30^\circ} \text{ V}$

$I_1 = \frac{E_1}{Z_{12}} = \frac{100 \cdot e^{j30^\circ}}{10 + j10} = 6,83 - j1,83 \text{ A}$

↓ po obrani



Po obrani: 1

Predmet neutralne tačke!

$$U_0 = \frac{E_1 Y_1 + E_2 Y_2 + E_3 Y_3}{Y_1 + Y_2 + Y_3} = \frac{100 \cdot e^{j30^\circ} \cdot Y_1 + 100 \cdot e^{j90^\circ} \cdot Y_2 + 100 \cdot e^{j150^\circ} \cdot Y_3}{Y_1 + Y_2 + Y_3}$$

$U_0 = j40 \text{ V}$

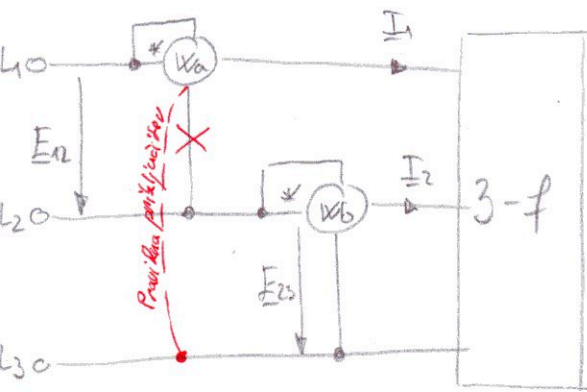
$Z_2 = 8 + j8 + \frac{(8 + j8)(8 + j8)}{16 + j16} = 14 + j14 \Omega$

$E_1 = E_1' - U_0$
 $E_1 = 100 \cdot e^{j30^\circ} - 40 \cdot e^{j90^\circ}$
 $E_1 = 87,18 \cdot e^{j6,59^\circ}$

$I_1 = \frac{E_1}{Z_1} = \frac{87,18 \cdot e^{j6,59^\circ}}{2 + j2} = 24,15 - j19,15 \text{ A}$



100V - punjenje



$$E_1 = 100 \cdot e^{j60^\circ} \text{ V}$$

$$I_1 = 2 - j3 \text{ A}$$

$$I_2 = 3 + j4 \text{ A}$$

S_a, S_b , punjenje
napuljenje

napuljenje!

$$E_{12} = E_1 \cdot \sqrt{3} \cdot e^{j30^\circ} = 100\sqrt{3} \cdot e^{j30^\circ} \text{ V}$$

$$E_{23} = E_{12} \cdot e^{j120^\circ} = 100\sqrt{3} \cdot e^{j210^\circ} \text{ V}$$

$$S_a = E_{12} \cdot I_1^* = 100\sqrt{3} \cdot e^{j30^\circ} \cdot (2 + j3) = \underbrace{559,81 + j276,2}_{P} \text{ VA}$$

$$S_b = E_{23} \cdot I_2^* = 100\sqrt{3} \cdot e^{j210^\circ} \cdot (3 - j4)$$

$$W_a = 559,81 \text{ W}$$

$$= -796,41 + j340,19 \text{ VA}$$

$$W_b = -796,41 \text{ W}$$

$$P_{\text{ostatak}} = W_a + W_b = -236,6 \text{ W}$$

punjenje!

W_b punjenje

$$S_a = E_{31} \cdot I_1^*$$

$$E_{31} = E_{23} \cdot e^{j120^\circ} = 100\sqrt{3} \cdot e^{j90^\circ}$$

$$S_a = -100\sqrt{3} \cdot e^{j90^\circ} \cdot (2 + j3)$$

$$E_{13} = -E_{31} = -100\sqrt{3} \cdot e^{j90^\circ} \text{ V}$$

$$S_a = 519,62 - j346,41 \text{ VA}$$

$$P_{\text{ost.}} = 1079,42 \text{ W}$$

