

#### 4. domača naloga iz Osnov elektrotehnike II

1. Transformator z nazivno močjo  $S_{nT}=500$  kVA je trenutno polno obremenjen z bremenom, ki ima  $\cos\varphi=0,6$ . Na transformator želimo priključiti še dodatno breme z delovno močjo  $P_d=100$  kW in  $\cos\varphi_d=0,9$ . Določite potrebno velikost kompenzacije  $Q_c$ , da bo transformator po kompenzaciji deloval s  $\cos\varphi_2=0,95$ .

2. Transformator z nazivno močjo  $S_{nT}=200$  kVA je trenutno polno obremenjen z bremenom, ki ima  $\cos\varphi=0,6$ . Na transformator želimo priključiti še dodatno breme, ki ima navidezno moč  $S_\Delta=60$  kVA in  $\cos\varphi_\Delta=0,8$ . Določite najmanjšo potrebno velikost kompenzacije  $Q_c$ , da transformator ne bo preobremenjen.

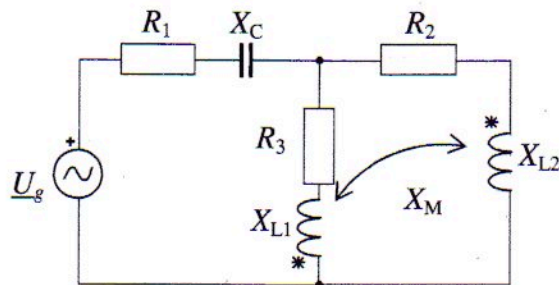
3. Izračunajte ekvivalentne elemente za zaporedno nadomestno vezavo realnega kondenzatorja s podatki:  $U = 400$  V,  $Q_C=4 \cdot 10^3$  var,  $\text{tg}\delta = 10^{-4}$ ,  $\omega = 2,5 \cdot 10^4$  rad/s.

4. Na realnem kondenzatorju smo pri napetosti  $U = 250$  V in frekvenci 50 Hz izmerili tok  $I = 0,1$  A ter izgube  $P = 12,5$  mW. Določite elemente nadomestne vzporedne vezave ( $R_{vz}$ ,  $C$  in  $\text{tg}\delta$ ).

5. V realni tuljavi z železnim jedrom smo pri napetosti  $U = 20$  V izmerili tok  $I = 2$  A in moč (izgube)  $P = 4$  W. Jedro odstranimo in izgube se pri istem toku zmanjšajo na 1 W. Določite elemente nadomestne vezave ( $z$  in brez jedra), če zanemarimo stresanje in je frekvenca 100 Hz.

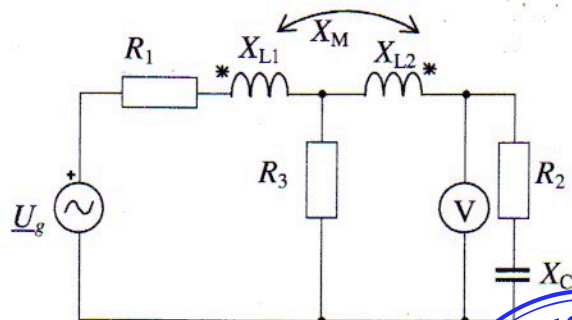
6. Na realni tuljavi (brez stresanja) smo pri napetosti  $U_1=80$  V izmerili tok  $I_1=6$  A in  $\cos\varphi_1=0,7$ . Nato v tuljavo vstavimo železno jedro in ponovimo meritve pri enaki napetosti. Izmerimo tok  $I_2=4$  A in  $\cos\varphi_2=0,9$ . Izračunajte izgube v bakru in železu ter reaktanco  $X_L$ .

7. Določite toke v vezju na sliki.  $\underline{U}_g = 70 - j110$  V,  $R_1 = 14 \Omega$ ,  $R_2 = 4 \Omega$ ,  $R_3 = 8 \Omega$ ,  $X_{L1} = 18 \Omega$ ,  $X_{L2} = 6 \Omega$ ,  $X_C = 12 \Omega$  in  $X_M = 6 \Omega$ .

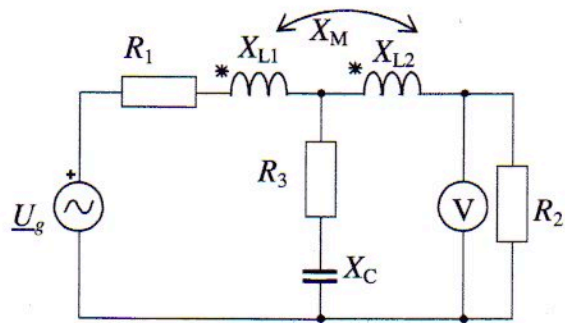


8. Kakšen bi moral biti  $X_c$  v vezju iz prejšnje naloge, da bi bilo vezje v napetostni resonanci.

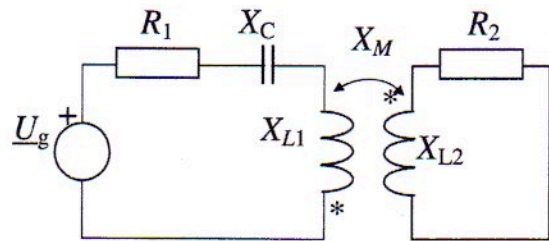
9. Določite napetost, ki jo meri voltmeter v vezavi na sliki.  $\underline{U}_g = 100 + j100$  V,  $R_1 = 5 \Omega$ ,  $R_2 = 5 \Omega$ ,  $R_3 = 10 \Omega$ ,  $X_{L1} = 15 \Omega$ ,  $X_{L2} = 20 \Omega$ ,  $X_C = 5 \Omega$  in  $X_M = 10 \Omega$ . (Voltmeter meri efektivno vrednost napetosti!)



10. Določite napetost, ki jo meri voltmeter v vezavi na sliki 1.  $\underline{U}_g = 100 + j200 \text{ V}$ ,  $R_1 = 5 \Omega$ ,  $R_2 = 10 \Omega$ ,  $R_3 = 5 \Omega$ ,  $X_{L1} = 20 \Omega$ ,  $X_{L2} = 15 \Omega$ ,  $X_C = 5 \Omega$  in  $X_M = 5 \Omega$ . (Voltmeter meri efektivno vrednost napetosti!)



11. V vezju na sliki določite  $X_C$  tako, da bo vezje v napetostni resonanci. Podatki elementov so:  $R_1 = 8 \Omega$ ,  $R_2 = 4 \Omega$ ,  $X_{L1} = 30 \Omega$ ,  $X_{L2} = 4 \Omega$ ,  $X_M = 3 \Omega$ .



Rešitve:

1.  $Q_C = 316,96 \text{ kvar}$
2.  $Q_{C,\min} = 87,48 \text{ kvar}$
3.  $R_z = 4 \cdot 10^{-3} \Omega$ ,  $C = 1 \mu\text{F}$
4.  $R_{vz} = 5 \text{ M}\Omega$ ,  $C = 1,27 \mu\text{F}$ ,  $\text{tg}\delta = 5 \cdot 10^{-4}$
5.  $R_{Cu} = 0,25 \Omega$ ,  $R_{Fe} = 0,75 \Omega$ ,  $L_0 = 15,8 \text{ mH}$
6.  $P_{Cu1} = 336 \text{ W}$ ,  $P_{Cu2} = 149,28 \text{ W}$ ,  $P_{Fe} = 139,2 \text{ W}$ ,  $R_{Cu} = 9,3 \Omega$ ,  $R_{Fe} = 8,7 \Omega$ ,  $X_L = 8,72 \Omega$
7.  $I_1 = 6 - j3 \text{ A}$ ,  $I_2 = 4 - j2 \text{ A}$ ,  $I_3 = 2 - j1 \text{ A}$
8.  $X_C = 2 \Omega$
9.  $\underline{U}_V = 40 - j40 \text{ V}$  ( $U_V = 56,57 \text{ V}$ )
10.  $\underline{U}_V = 10,07 - j57,05 \text{ V}$  ( $U_V = 57,93 \text{ V}$ )
11.  $X_C = 28,875 \Omega$

u DN / A. nal.)

$$S_{NT} = 500 \text{ kVA} = S_1$$

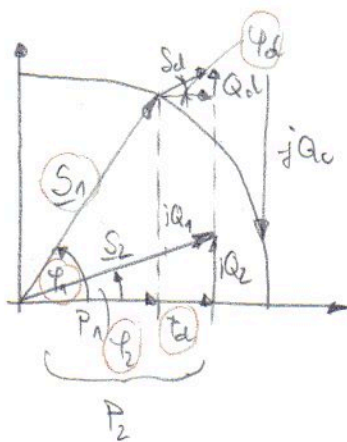
$$\cos \varphi_1 = 0,6$$

$$P_d = 100 \text{ kVA}$$

$$\cos \varphi_d = 0,9$$

$$\cos \varphi_2 = 0,95$$

$Q_c = ?$  da bo



$$Q_c = Q_1 + Q_d - Q_2$$

$$\sin \varphi_1 = 0,8$$

$$P_1 = S_1 \cdot \cos \varphi_1 = 500 \cdot 0,6 = \boxed{300 \text{ kW}}$$

$$P_2 = P_1 + P_d = 300 + 100 = \boxed{400 \text{ kW}}$$

$$Q_1 = \sin \varphi_1 \cdot S_1 = 0,8 \cdot 500 = \boxed{400 \text{ kvar}}$$

$$Q_d = \tan \varphi_d \cdot P_d = \boxed{48,432 \text{ kvar}}$$

$$Q_2 = \tan \varphi_2 \cdot P_2 = \boxed{131,474 \text{ kvar}}$$

$$Q_c = Q_1 + Q_d - Q_2$$

$$Q_c = 400 + 48,432 - 131,474 = \boxed{316,96 \text{ kvar}}$$



2.

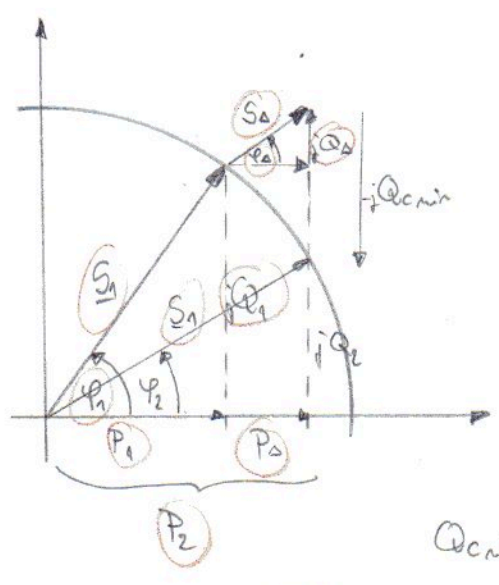
Postupno cBR.  
 $S_{NT} = 200 \text{ kVA} = S_1$

$\cos \varphi_1 = 0,6$

$S_\Delta = 60 \text{ kVA}$

$\cos \varphi_\Delta = 0,8$

$Q_{cmin} = ?$



$Q_{cmin} = Q_1 + Q_\Delta - Q_2$

$P_1 = \cos \varphi_1 \cdot S_1 = 120 \text{ kW}$

$Q_{cmin} = 87,48 \text{ kvar}$

$Q_1 = \sin \varphi_1 \cdot S_1 = 160 \text{ kvar}$

$Q_\Delta = \sin \varphi_\Delta \cdot S_\Delta = 36 \text{ kvar}$

$P_\Delta = \cos \varphi_\Delta \cdot S_\Delta = 48 \text{ kW}$

$Q_2 = \sqrt{S_1^2 - P_2^2}$

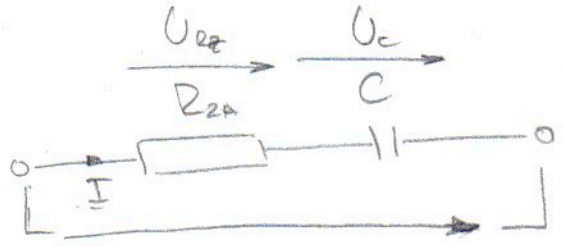
$P_2 = P_1 + P_\Delta = 168 \text{ kW}$

$Q_2 = 108,52 \text{ kvar}$



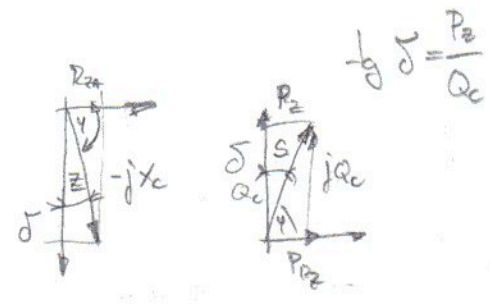
3.

$U = 400 \text{ V}$   
 $Q_c = 4 \cdot 10^8 \text{ var}$   
 $\text{tg } \delta = 1 \cdot 10^{-4}$   
 $\omega = 2,5 \cdot 10^4 \text{ rad/s}$



$R_{2A}, C = ?$

$U \approx U_c$   
 $S \approx Q_c$



$$X_c = \frac{U_c}{I} = \frac{400}{10} = 40 \Omega$$

$$Q_c = U_c \cdot I$$

$$I = \frac{Q_c}{U_c} = \frac{4 \cdot 10^8}{400} = 10 \text{ A}$$

$$C = \frac{1}{\omega X_c} = \frac{1}{2,5 \cdot 10^4 \cdot 40} = 1 \cdot 10^{-6} \text{ F} = 1 \mu\text{F}$$

$$P_{2A} = \text{tg } \delta \cdot Q_c = 0,4 \text{ W}$$

$$P_{2A} = U \cdot I = I^2 \cdot R_{2A} \Rightarrow R_{2A} = \frac{P_{2A}}{I^2} = \frac{4 \cdot 10^{-1}}{100} = 4 \cdot 10^{-3} \Omega$$

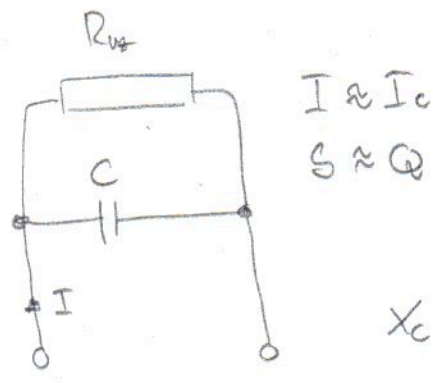


4.

$U = 250 \text{ V}$   
 $f = 50 \text{ Hz}$   
 $I = 0,1 \text{ A}$   
 $P = 12,5 \text{ mW}$   


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 $R_{rz}, C, \text{tg } \delta = ?$



$$X_c = \frac{U_c}{I_c} = \frac{250}{1 \cdot 10^{-1}} = \boxed{2500 \Omega}$$

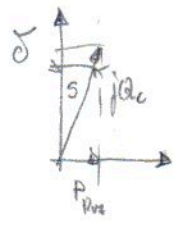
$$C = \frac{1}{\omega X_c} = \frac{1}{50 \cdot 2\pi \cdot 2,5 \cdot 10^3} = \boxed{1,273 \mu\text{F}}$$

$$P = U \cdot I = \frac{U^2}{R_{rz}} \Rightarrow R_{rz} = \frac{U^2}{P} = \frac{250^2}{12,5 \cdot 10^{-3}} = \boxed{5 \text{ M}\Omega}$$

$$\text{tg } \delta = \frac{12,5 \cdot 10^{-3}}{25} = \boxed{5 \cdot 10^{-4}}$$

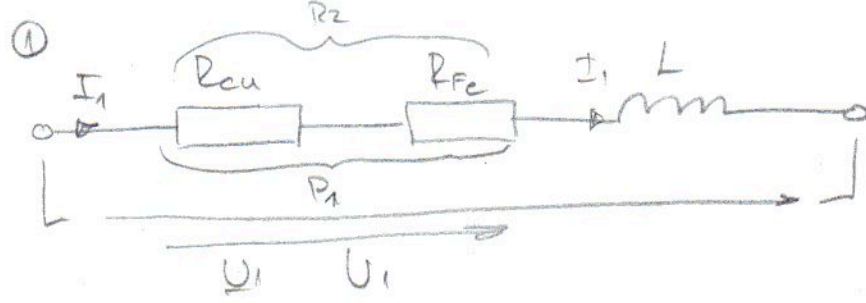
$$S = U \cdot I = 250 \cdot 0,1$$

$$S = \boxed{25 \text{ VA}} \approx Q$$



$$\text{tg } \delta = \frac{P}{Q_c}$$

⑤ ① Z, Fe U <sub>1</sub> = 20V I <sub>1</sub> = 2A P <sub>1</sub> = 4W f = 1000 Hz	② Brez Fe I <sub>2</sub> = 2A P <sub>2</sub> = 1W
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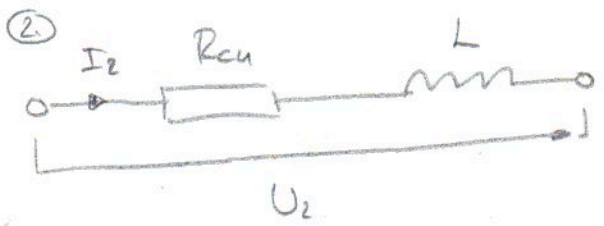
R<sub>cu</sub>, L, R<sub>Fe</sub>

$$P_{Fe} = P_1 - P_2 = \boxed{3W}$$

$$P_1 = U \cdot I = I_1^2 R_2$$

$$R_2 = \frac{P_1}{I_1^2} = \boxed{1\Omega}$$

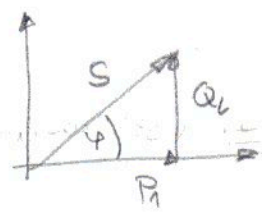
$$R_{cu} = R_2 - R_{Fe} = \boxed{0,25\Omega}$$



$$S = U \cdot I = \boxed{40VA}$$

$$P_{Fe} = I_2 U = I_2^2 R_{Fe}$$

$$\Rightarrow R_{Fe} = \frac{P_{cu}}{I_2^2} = \frac{3}{2^2} = \boxed{0,75\Omega}$$

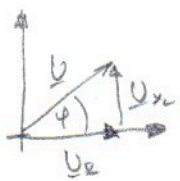


$$\cos \varphi = \frac{P_1}{S} \Rightarrow \varphi = \boxed{84,26^\circ}$$

$$Q_c = \sin \varphi \cdot S = \boxed{39,8 \text{ var}}$$

$$X_L = \frac{U_{Lc}}{I_2} = \boxed{9,949\Omega}$$

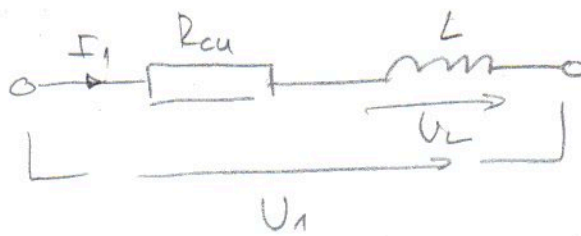
$$L = \frac{X_L}{\omega} = \boxed{15,835 \text{ mH}}$$



$$U_{Lc} = \sin \varphi \cdot U$$

$$U_{Lc} = \boxed{19,899V}$$

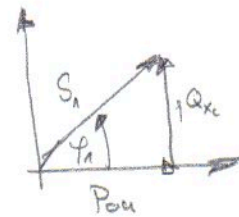
$U_1 = 80V$ $I_1 = 6A$ $\cos \varphi_1 = 0,7$	$Z = Fe$ $U_2 = 80V$ $I_2 = 4A$ $\cos \varphi_2 = 0,9$
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$$S_1 = U \cdot I_1 = \boxed{480 VA}$$

$$P_{cu1} = \cos \varphi_1 \cdot S_1$$

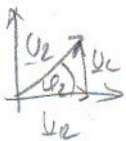
$$P_{cu1} = \boxed{336 W}$$



$$Q_{xL} = \sin \varphi_1 \cdot S_1$$

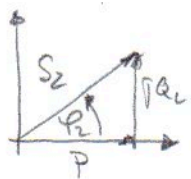
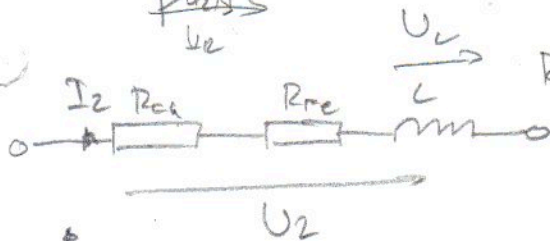
$$Q_{xL} = \boxed{342,79 var}$$

$$U_L = \sin \varphi_2 \cdot U_2 = \boxed{34,87V}$$



$$P_{cu1} = U_{cu1} \cdot I_{cu1} = I_{cu1}^2 R_{cu1}$$

$$R_{cu1} = \frac{P_{cu1}}{I_{cu1}^2} = \boxed{9,33 \Omega}$$



$$S_2 = U_2 \cdot I_2 = \boxed{320 VA}$$

$$P_{cu2} = U_{cu2} \cdot I_{cu2} = I_{cu2}^2 R_{cu2}$$

$$P_{cu2} = \boxed{149,33 W}$$

$$P = P_{cu2} + P_{Fe}$$

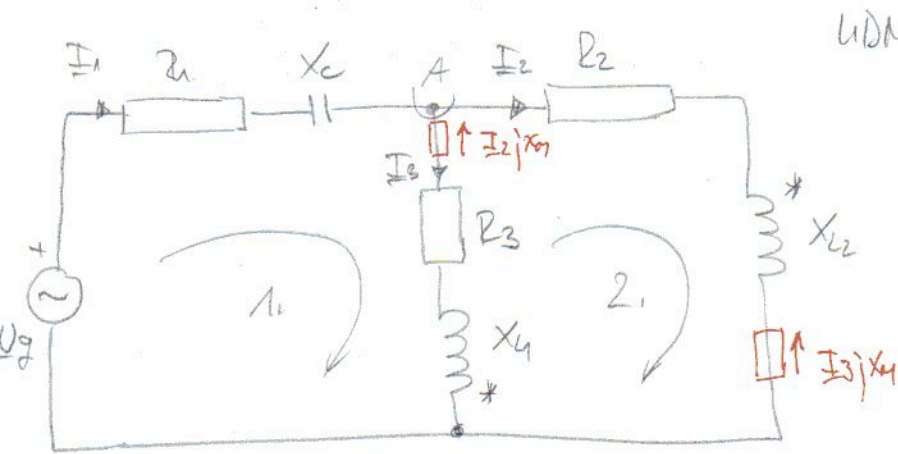
$$P = \cos \varphi_2 \cdot S_2 = \boxed{288 W}$$

$$P_{Fe} = P - P_{cu2} = \boxed{138,67 W}$$

$$P_{Fe} = I_{Fe}^2 \cdot R_{Fe} \Rightarrow R_{Fe} = \frac{P_{Fe}}{I_{Fe}^2} = \boxed{8,67 \Omega}$$

$$X_L = \frac{U_L}{I_L} = \boxed{8,72 \Omega}$$





UDN/7 final

$$U_g = 70 - j110 \text{ V}$$

$$R_1 = 14 \Omega \quad X_1 = 18 \Omega$$

$$R_2 = 4 \Omega \quad X_2 = 6 \Omega$$

$$R_3 = 8 \Omega$$

$$X_c = 12 \Omega$$

$$X_n = 6 \Omega$$

$$1) \quad I_1(R_1 - jX_c) - I_2 jX_M + I_3(R_3 + jX_4) = U_g$$

$$2) \quad I_2(R_2 + jX_{L2} + jX_M) - I_3(jX_M + jX_4 + R_3) = 0$$

$$A: \quad I_1 = I_2 + I_3$$

$$I_3 = \frac{I_2(R_2 + jX_{L2} + jX_M)}{jX_M + jX_4 + R_3}$$

$$I_1 = I_2 \left( 1 + \frac{R_2 + jX_{L2} + jX_M}{jX_M + jX_4 + R_3} \right)$$

$$I_1 = I_2 \left( 1 + \frac{4 + j12}{8 + j24} \right)$$

$$I_1 = I_2 \left( \frac{3 + j3}{2 + j2} \right) = I_2 \left( \frac{3}{2} \right)$$

$$I_2 \left( \frac{42 - j36}{2} - j6 + \frac{(4 + j12)(8 + j18)}{8 + j24} \right) = 70 - j110 \text{ V}$$

$$I_1 = \frac{3}{2} I_2$$

$$I_1 = \frac{3 \cdot (4 - j2)}{2}$$

$$= \frac{12 - j6}{2} = \boxed{6 - j3 \text{ A}}$$

$$I_2 \left( 21 - j18 - j6 + \frac{32 + j72 + j96 - 216}{8 + j24} \right) = 70 - j110 \text{ V}$$

$$I_2 \left( 21 - j24 + \frac{2560 + j5760}{640} \right) = 70 - j110 \text{ V}$$

$$I_3 = I_1 - I_2$$

$$I_3 = 6 - j3 - 4 + j2 = \boxed{2 - j1 \text{ A}}$$

$$I_2 = \frac{70 - j110}{25 - j15} = \boxed{4 - j2 \text{ A}}$$



8. LON

$$1) \underline{I}_1 (R_1 - jX_C) - \underline{I}_2 jX_M + \underline{I}_3 (R_3 + jX_{L1}) = \underline{U}_g$$

$$\underline{I}_1 = \underline{I}_2 + \underline{I}_3$$

$$2) \underline{I}_2 (R_2 + jX_{L2} + jX_{L1}) - \underline{I}_3 (jX_M + jX_{L1} + R_3) = 0$$

$$\underline{I}_3 = \underline{I}_1 - \frac{2}{3} \underline{I}_1$$

$$\underline{I} \left( \frac{\underline{U}_g}{\underline{I}_1} \right) = 0$$

$$\underline{I}_1 = \frac{3}{2} \underline{I}_2 \Rightarrow \underline{I}_2 = \frac{2}{3} \underline{I}_1$$

$$\underline{I}_3 = \frac{1}{3} \underline{I}_1$$

$$\underline{I}_1 (R_1 - jX_C) - \frac{2}{3} \underline{I}_1 jX_M + \frac{1}{3} \underline{I}_1 (R_3 + jX_{L1}) = \underline{U}_g$$

$$\frac{\underline{U}_g}{\underline{I}_1} = R_1 - jX_C - \frac{2jX_M}{3} + \frac{R_3 + jX_{L1}}{3}$$

$$\frac{\underline{U}_g}{\underline{I}_1} = 14 - jX_C - j4 + \frac{8 + j18}{3}$$

$$\operatorname{Im} \left( \frac{\underline{U}_g}{\underline{I}_1} \right) = 0$$

$$-X_C - 4 + \frac{18}{3} = 0$$

$$X_C = \frac{18}{3} - \frac{12}{3}$$

$$X_C = 2 \Omega$$

9.

A)  $I_1 = I_2 + I_3$

1)  $I_1(R_1 + jX_{L1}) - I_2 jX_M + I_3 R_3 = U_g$

2)  $-I_1 jX_M + I_2(jX_{L2} + R_2 - jX_C) - I_3 R_3 = 0$

$I_1(5 + j15 - j10) + I_2(20 + j5 - j5 - j10) = U_g$

$I_1(5 + j5) + I_2(5 + j5) = 100 + j100$

$\frac{(5 + j5)(I_1(10 + j10) + (100 + j100))}{15 + j15} + I_2(5 + j5) = 100 + j100$   
 $I_3 = \frac{I_2 jX_M - I_1(R_1 + jX_{L1}) + U_g}{R_3}$

$(5 + j5)(I_2(10 + j10) + (100 + j100)) + I_2 j150 = j3000$

$I_2 j100 + j1000 + I_2 j150 = j3000$

$I_2(j100 + j150) = j2000$

$I_2 = 8 A$

$U_v = I_2 \cdot (R_2 + jX_C)$

$U_v = 8 \cdot (5 - j5) = 40 - j40 V$

$U_v = 40 \cdot \sqrt{2} V = 56,57 V$

$I_1 = I_2 + \frac{I_2 jX_M - I_1(R_1 + jX_{L1}) + U_g}{R_3}$

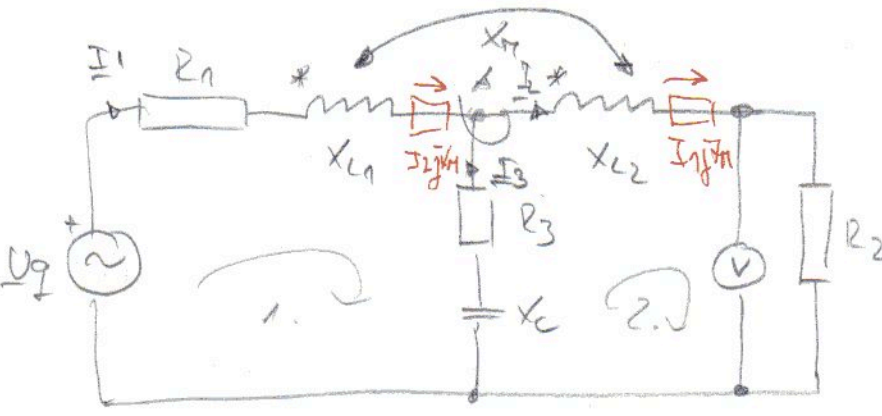
$I_1 R_3 + I_1(R_1 + jX_{L1}) = I_2(R_3 + jX_M) + U_g$

$I_1 = \frac{I_2(R_3 + jX_M) + U_g}{R_3 + R_1 + jX_{L1}}$

$I_1 = \frac{I_2(10 + j10) + U_g}{15 + j15}$

$I_1 = \frac{I_2(10 + j10) + (100 + j100)}{15 + j15}$





$$U_g = 100 + j200$$

$$R_1 = 5 \Omega$$

$$R_2 = 10 \Omega$$

$$R_3 = 5 \Omega$$

$$X_{L1} = 20 \Omega$$

$$X_{L2} = 15 \Omega$$

$$X_C = 5 \Omega$$

$$X_M = 5 \Omega$$

10.

A:  $I_1 = I_2 + I_3$

1)  $I_1(R_1 + jX_{L1}) + I_2 jX_M + I_3(R_3 - jX_C) = U_g$

2)  $I_1 jX_M + I_2(R_2 + jX_{L2}) - I_3(R_3 - jX_C) = 0 \Rightarrow I_3 = \frac{I_1 jX_M + I_2(R_2 + jX_{L2})}{R_3 - jX_C}$

$I_1(5 + j20 + j5) + I_2(10 + j15 + j5) = 100 + j200$

3)  $I_1 = I_2 + I_3$

$I_2 \frac{(-1 + j8)(5 + j25)}{5} + I_2(10 + j20) = 100 + j200$

$I_1 = I_2 + \frac{I_1 jX_M + I_2(R_2 + jX_{L2})}{R_3 - jX_C}$

$I_2(-4 + j3 + 10 + j20) = 100 + j200$

$I_1(R_3 - jX_C - jX_M) = I_2(R_2 + jX_{L2} + R_3 - jX_C)$

$I_2 = \frac{100 + j200}{-31 + j23} = 1,0067 + j5,705A$

$I_1 = \frac{(R_2 + jX_{L2} + R_3 - jX_C) I_2}{R_3 - jX_C - jX_M}$

$I_1 = \frac{I_2(15 + j10)}{5 - j10} = \frac{I_2(-1 + j8)}{5}$

$U_v = I_2 \cdot R_2 = 10,067 - j57,047V$

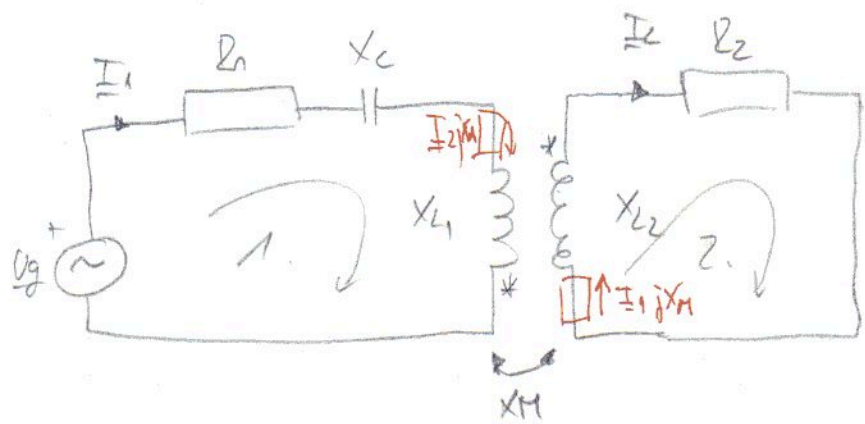
$U_v = 57,93V$

A:  $\begin{bmatrix} (5, 20) & (0, 5) & (5, -5) \\ (0, 5) & (10, 15) & (-5, 5) \\ (-1, 0) & (1, 0) & (1, 0) \end{bmatrix}$

B:  $\begin{bmatrix} (100, 200) \\ (0, 0) \\ (0, 0) \end{bmatrix}$







- $R_1 = 8 \Omega$
- $R_2 = 4 \Omega$
- $X_{L1} = 30 \Omega$
- $X_{L2} = 4 \Omega$
- $X_M = 3 \Omega$



$$\text{Im} \left( \frac{U_g}{I_1} \right) = \phi$$

$$1) I_1 (R_1 + jX_C + jX_{L1}) + I_2 jX_M = U_g$$

$$2) I_2 (R_2 + jX_{L2}) + I_1 jX_M = 0 \rightarrow I_2 = \frac{-I_1 jX_M}{R_2 + jX_{L2}}$$

$$I_1 (R_1 - jX_C + jX_{L1}) + \frac{-I_1 X_M^2}{R_2 + jX_{L2}} = U_g$$

$$I_1 \left( R_1 - jX_C + jX_{L1} + \frac{-X_M^2}{R_2 + jX_{L2}} \right) = U_g$$

$$\frac{U_g}{I_1} = R_1 - jX_C + jX_{L1} + \frac{-X_M^2}{R_2 + jX_{L2}}$$

$$\text{Im} \left( \frac{U_g}{I_1} \right) = \phi$$

$$-jX_C + jX_{L1} + \frac{-X_M^2}{R_2 + jX_{L2}} = \phi$$

$$X_C = X_{L1} + \frac{X_M^2}{R_2 + X_{L2}}$$

Dengan cara →



$$1.) \underline{I}_1 (R_1 - jX_C + jX_{L1}) + \underline{I}_2 jX_M = U_g$$

$$2.) \underline{I}_1 jX_M + \underline{I}_2 (R_2 + jX_{L2}) = 0 \Rightarrow \underline{I}_2 = \frac{-\underline{I}_1 jX_M}{R_2 + jX_{L2}}$$

$$\underline{I}_1 (R_1 - jX_C + jX_{L1}) + jX_M \cdot \frac{-\underline{I}_1 jX_M}{R_2 + jX_{L2}} = U_g$$

$$\underline{I}_1 (R_1 - jX_C + jX_{L1}) + \frac{\underline{I}_1 X_M^2}{R_2 + jX_{L2}} = U_g$$

$$\underline{I}_1 \cdot \left( R_1 - jX_C + jX_{L1} + \frac{X_M^2}{R_2 + jX_{L2}} \right) = U_g$$

$$\frac{U_g}{\underline{I}_1} = R_1 - jX_C + jX_{L1} + \frac{X_M^2 (R_2 - jX_{L2})}{R_2^2 + X_{L2}^2}$$

$$\operatorname{Im} \left( \frac{U_g}{\underline{I}_1} \right) = 0$$

$$-jX_C + jX_{L1} + \frac{-jX_{L2} X_M^2}{R_2^2 + X_{L2}^2} = 0$$

$$X_C = X_{L1} + \frac{-X_{L2} X_M^2}{R_2^2 + X_{L2}^2}$$

$$X_C = 30 + \frac{-4 \cdot 3^2}{4^2 + 4^2} = 30 + \frac{-36}{32} = \boxed{28,875 \Omega}$$